

**ICS 271**  
**Fall 2018**  
**Instructor : Kalev Kask**  
**Homework Assignment 2**  
**Due Saturday 10/20**

1. (10 points) Suppose that we run a best-first search algorithm with the following evaluation functions,
  - (a)  $f(n) = -g(n)$ . What sort of search will this search emulate?
  - (b)  $f(n) = g(n)$ . What sort of search will this search emulate?
2. (10 points) Trace the operation of graph-search  $A^*$  applied to the problem of getting to Bucharest from Zerind using the straight-line distance heuristic. That is, show the frontier at each step, nodes that the algorithm will expand and the  $f$ ,  $g$  and  $h$  value for each node.
3. (50 points) Which of the following are true and which are false? Explain your answers.
  - (a) Depth-first search always expands at least as many nodes as  $A^*$  search with an admissible heuristic.
  - (b)  $h(n) = 0$  is an admissible heuristic for the 8-puzzle.
  - (c)  $A^*$  is of no use in robotics because percepts, states, and actions are continuous.
  - (d) Breadth-first search is complete even if zero step costs are allowed.
  - (e) Assume that a rook can move on a chessboard any number of squares in a straight line, vertically or horizontally, but cannot jump over other pieces. Manhattan distance is an admissible heuristic for the problem of moving the rook from square A to square B in the smallest number of moves.
4. (50 points) A heuristic function is consistent if for every node  $n$  and its child node  $n'$ ,  $h(n) \leq c(n, n') + h(n')$ . Prove the following properties of algorithm  $A^*$ .
  - (a) (10) The  $f$ -values of the nodes expanded by Best-First-Search form a non-decreasing sequence.

- (b) (10) Prove that if  $h_1$  and  $h_2$  are both consistent, so also is  $h = \max(h_1, h_2)$ .
  - (c) (10) Prove that if  $h$  is consistent then it is also admissible (hint, you can prove this by induction moving from the goal node backwards).
  - (d) (10) Prove that if the heuristic function is consistent then  $A^*$  graph search will never re-open any nodes.
  - (e) (10) Prove or give a counter example: if for every node  $n$ ,  $h_1(n) \geq h_2(n)$ , and for some nodes  $h_1(n) > h_2(n)$  then  $A^*$  with  $h_1$  always expands less nodes than  $A^*$  with  $h_2$ .
5. (15 points) Prove each of the following statements, or give a counterexample:
- (a) Breadth-first search is a special case of uniform-cost search.
  - (b) Depth-first search is a special case of best-first tree search.
  - (c) Uniform-cost search is a special case of  $A^*$  search.